# Astron 211 Problem Set 9

Given: Nov 15. Due: Nov 22 at the beginning of class

**Homework Policy:** You can consult class notes and books. Always try to solve the problems yourself; if you cannot make progress after some effort, you can discuss with your classmates or ask the instructor. However, you cannot copy other's work: what you turn in must be your own. Make sure you are clear about the process you use to solve the problems: partial credit will be awarded.

**Reading:** Kutner Chapter 22–25, 4

#### Problem 1 Kutner Problem 22.11

How does the kinetic energy of an object with the escape speed at a distance r from a mass M compare with that of an object in a circular orbit of radius r?

#### Problem 2 Kutner Problem 23.6

Express the equilibrium temperature of a planet as a function of that of the Earth and the distance of the planet from the Sun in astronomical units. In other words, we want an equation:

$$T = f(T_{\oplus}, a)$$

where a is expressed in AU. Use your equation to construct a table of the equilibrium temperatures for the 8 planets.

#### Problem 3 Kutner Problem 24.5

The law of hydrostatic equilibrium is:

$$\frac{\Delta P}{\Delta r} = -g\rho$$

where  $\Delta P$  is the change in pressure and  $\Delta r$  the change in radius between two points.

Use this to compute how far under water do we have to go on Earth to obtain a pressure of 90 atmospheres?

### Problem 4 Kutner Problem 25.5

What is the ratio of solar energy per second per unit surface area (i.e.,  $W/m^2$ ) reaching Uranus to that reaching Neptune?

#### Problem 5 Kutner Problem 4.2

Estimate the angular resolution of a  $5 \,\mathrm{m}$  diameter optical telescope in space.

### Problem 6 Kutner Problem 4.16

What is the angular resolution of HST at 200 nm wavelength?

#### Problem 7 Kutner Problem 4.22

Two infrared sources in the Orion Nebula are 500 pc from us and are separated by 0.1 pc. How large a telescope would you need to distinguish the sources at a wavelength of 100  $\mu$ m?

## Problem 8 Kutner Problem 4.26

Two infrared sources in the Orion Nebula are 500 pc from us and are separated by 0.1 pc. How large a telescope would you need to distinguish the sources at a wavelength of (a) 21 cm? (b) 1 mm?

### Problem 9 Order of Magnitude: Tea

Radio astronomy started in earnest in the 1960's with the construction of the 300-m Arecibo Telescope. Strong sources have flux densities of about 1 Jansky, or  $10^{-26}$  W/m<sup>2</sup>/Hz. Assume that a radio telescope can add up the signal over a bandwidth of 100 MHz, how much energy total has been received by the Arecibo Observatory since it started? Would this boil a cup of tea?